

Asymmetric Properties of Office Rent Adjustment

Dirk Brounen · Maarten Jennen

Published online: 20 May 2009

© The Author(s) 2009. This article is published with open access at Springerlink.com

Abstract In this paper we use an error correction model for understanding the changes in real office rents for a panel of 15 U.S. MSA's over the period 1990–2007. We find that office rents in all cities react positively to a rise in office employment and lagged rent changes, while lagged deviations from equilibrium rent levels exhibit a slow and partial adjustment over time. Given the non-negativity constraint of vacancy rates we extend the basic model by examining whether rents react to positive changes in employment conditional on the vacancy rate level. Our results show that office rents react significantly stronger to increases in employment when vacancy rates are below the long-term average. We also repeat the analysis for clusters of cities based on similarities in rent and employment dynamics using multi dimensional scaling. The cluster results confirm the overall conclusions and show that our results are not solely valid for the full panel of cities.

Keywords Office rents · Error correction model · Panel data

Introduction

In this study we show that the impact of increases in demand for office space on changes in office rents depends on the disequilibrium in the demand-supply relationship. If vacancy rates are below their long term average office rents react significantly stronger to positive changes in office employment when compared to periods of abundant supply. Understanding rent dynamics is key to both users and investors in office markets, markets that have developed into a significant proportion of the overall economy. According to the U.S. Bureau of Labor Statistics office employment accounts for over 19% of non-farm employment. This statistic represents a total of 26 million office based employees

D. Brounen · M. Jennen (✉)

Rotterdam School of Management, Erasmus University, Burg. Oudlaan 50, 3062 PA, Rotterdam,
The Netherlands
e-mail: mjennen@rsm.nl

D. Brounen
e-mail: dbrounen@rsm.nl

M. Jennen
ING Real Estate, Schenkade 65, p.o. Box 90463, 2509 LL, The Hague, The Netherlands

in the U.S. by the end of 2007. For metropolitan areas like San Francisco, Washington DC and New York the weight of office employment can reach peaks of close to 30%.

Office rents are also a key input variable for construction decisions and to a large extent determine the profitability of new office investments. Hence, a vast strand of academic literature has developed over the years, which aims at cracking the DNA code of office rents. In these models, rents are typically related to changes in employment, office supply and vacancy levels. However, in almost all of these studies the authors assume that these relationships are symmetric, and thus that changes in employment will have similar scale effects irrespective of the level of the vacancy rate. Early studies by Wheaton (1987) already showed that vacancy rates evolve around a natural rate, and that given the non-negativity constraint vacancy rates tend to reach more distinctive peaks than troughs. Therefore, an increase in office employment, when vacancy rates are low, is likely to have a very different impact on rents, than when rates are high. Englund et al. (2008a) are the first to include these asymmetric properties into their model calibration. They explicitly studied asymmetric rent adjustments depending on the level of vacancy rates when modeling Stockholm office rents for the period 1977–2002 and reported a significant increase in the explanatory power of their rent models due to this inclusion.

This paper will add to the existing literature by applying an asymmetric rent adjustment model to a unique panel set of quarterly data that covers fifteen metropolitan areas (MSA's) in the United States over the period 1990–2007. Measured by net rentable area of office floor space these MSA's are the largest in the U.S. and include Atlanta, Boston, Chicago, Dallas, Denver, Detroit, Houston, Los Angeles, Minneapolis, New York, Philadelphia, Pittsburgh, San Francisco and Washington DC. Besides a panel that includes all MSA's in one specification we also estimate the model based on different clusters. We group MSA's with multi dimensional scaling based on similarity in rent- or employment dynamics and run panel data regressions based on these clusters. The clustering methodology benefits from an increase in the number of observations when compared to analysis on a MSA level while keeping the in-group homogeneity as large as possible. Our results show that changes in office employment have a larger impact on office rents when vacancy rates are below their long term average. This finding implies for office investments that new demand does not influence rent rates in a symmetric way but is most influential when prevailing vacancy rates are relatively low. We also show that the coefficients are similar in sign and magnitude across clusters.

The paper continues as follows. After discussing the office market literature that is most relevant for our research, we discuss the rent adjustment model that will be applied in the subsequent analysis. Before discussing our results, we first present our dataset and review the main attributes of the markets that are included in our sample. In our results we explicitly compare results that were yielded from competitive model specifications; models with and without asymmetric properties. Besides discussing pooled panel results we also look at results, for clusters of cities. The main results will be summarized in our conclusions.

Modeling Office Rent Adjustments

The earliest office literature focused on vacancy rates and typically modelled office rent dynamics as a function of deviations from the natural vacancy rate that is

required to clear the market. Wheaton and Torto (1988) use U.S. national time series data on office rent levels and vacancy rates and find that excess vacancy rates affect real rents, while the natural vacancy rate is influenced by variables such as the local tenant structure, average lease terms in the market, expected absorption rates and operating costs. The main problem with this specification is the assumption that office rents keep on decreasing as long as the prevailing vacancy rate is above the perceived natural rate which does not fit actual relationships. Hendershott (1996), in a study of the Sydney office market, introduced a more general rent adjustment model in which changes in real rents are a function of vacancy and rent deviations from equilibrium levels. Equation 1 shows the basic form of this type of real estate rent modelling.

$$\% \Delta R_t = \alpha(v_t^* - v_{t-1}) + \beta(R_t^* - R_{t-1}) \quad (1)$$

Where v_t^* is the estimated natural vacancy rate and R_t^* is the time-varying equilibrium real office rent. This model offers a more general adjustment path for office rents with pleasing long-run properties, as effective rents are specified as adjustments to gaps between both the natural and actual vacancy rates and equilibrium and actual gross rents. With this equation, vacancy rates do not have to overshoot following a supply shock. After high vacancy rates have dragged rents significantly below equilibrium, the known eventual return to equilibrium acts as a force causing real rents to rise, even when the vacancy rate is still above the natural rate. This model is estimated by Hendershott et al. (1999) using data from the City of London for the period 1977-1996 and shows that the model tracks the market dynamics.

Hendershott et al. (2002) and Hendershott et al. (2002) extend these rent adjustment models by deriving a model that incorporates supply and demand factors within an Error Correction Model (ECM). This model is derived as a reduced-form estimation equation for the occupied office space and has the benefit that it does not require estimates for variables such as depreciation rates and operating expenses as is shown in Hendershott et al. (2002) where both a rent adjustment equation in line with Eq. 1 and an error correction model are estimated. Demand for space (D) is modelled as a function of real effective rent (R) and a proxy for office employment (E)¹:

$$D = \lambda_0 R^{\lambda_1} E^{\lambda_2} \quad (2)$$

Where the λ_i 's are constants with the price elasticity, λ_1 , expected to be negative and λ_2 , the income elasticity, positive. Demand for office space, a function of R and E as in Eq. 2, equals the product of available office space (SU) and one minus the prevailing office vacancy rate (v):

$$D(R, E) = (1 - v)SU \quad (3)$$

Given the fact that real estate markets clear towards equilibrium through changes in rents and vacancy levels (as shown in Eq. 3), vacancy enters the error correction model as a fitted variable indicated as \hat{v} in order to prevent endogeneity problems.

¹ In the data section we elaborate on the definition of office related employment.

The procedure we use to model vacancy levels is in line with Hendershott et al. (2002) and consists of an AR(4) model based on quarterly observations. Adjusted R^2 for the ten cities included in our analysis of the AR(4) model over the period 1990–2006 range from 0.93 to 0.95. Rearranging Eqs. (2) and (3) by logarithmic transformation, including fitted vacancy levels, and extracting real rent levels results in Eq. (4).

$$\ln R_{i,t} = \gamma_0 + \gamma_1 \ln E_{i,t} + \gamma_2 \ln [(1 - \hat{v}_{i,t})SU_{i,t}] + u_{i,t} \quad (4)$$

Where the subscripts i and t denote individual MSA's and quarters respectively. The ECM which is used to model changes in real prime rents in a panel data approach estimates long run equilibrium relationships and short-term corrections. Due to frictions, as already indicated by Wheaton (1987) in a study of the cyclic behaviour of the U.S. office market, office markets usually do not clear within short-run periods of time. We measure this imbalance as the residual of Eq. 4 and subsequently introduce this variable as a factor in the short-run model. The rationale for including the residual in the rent adjustment model is the delay in restoration of equilibriums in real estate markets due to factors such as long term contracts and high search costs. Equation 5 shows the disequilibrium.

$$u_{i,t} = \ln R_{i,t} - \gamma_0 - \gamma_1 \ln E_{i,t} - \gamma_2 \ln [(1 - \hat{v}_{i,t})SU_{i,t}] \quad (5)$$

Inclusion of the dependent variable in Eq. 5 in the rent adjustment model is possible if the variable is stationary which is equal to the independent variables being cointegrated. Since we base our model on panel data we apply the Levin et al. (2002) panel unit root test.²

Taking log differences of Eq. 4 and adding the stationary residual from Eq. 5 leads to the short-run rent adjustment model as depicted in Eq. 6 with an added lagged dependent variable to include the autoregression present in the change in real rent series.³

$$\begin{aligned} \Delta \ln R_{i,t} = & \alpha_0 + \alpha_1 \Delta \ln E_{i,t} + \alpha_2 \Delta \ln [(1 - \hat{v}_{i,t})SU_{i,t}] + \alpha_3 u_{i,t-1} \\ & + \alpha_4 \Delta \ln R_{i,t-1} + \varepsilon_{i,t} \end{aligned} \quad (6)$$

According to Eq. (6) office rents react to short-run changes in causal variables and to lagged residuals of the long-run model, as a reflection of market imbalances.⁴ The immediate responses to employment shocks and changes in occupied space are given by the coefficients α_1 and α_2 .

We use an extended version of Eq. 6 to capture the asymmetry in office rent adjustments. By including an interaction term between changes in $\ln E_t$ and a dummy variable, that takes value 1 if the vacancy rate is below the MSA long term average

² Tests for the presence of a unit root in the regression error terms shows that all residuals used in our study are stationary.

³ A regression of rent changes on rent changes lagged one period result in a coefficient of 0.32 which is significant at the 1% level.

⁴ Modelling results are expected to indicate that α_0 equals zero, α_1 , α_2 , α_3 and α_5 are positive, while, α_4 is expected to display a negative sign. α_3 indicates the speed of adjustment towards equilibrium. If α_3 equals -1 there is full equilibrium restoration after one period while α_3 between zero and -1 or larger than -1 indicate partial- and over- adjustment respectively.

vacancy rate and the change in office employment positive, and 0 otherwise, we test the hypothesis that office rents react stronger to changes in office employment when the market is tight. This results in the following rent adjustment equation:

$$\begin{aligned} \Delta \ln R_{i,t} = & \alpha_0 + \alpha_1 \Delta \ln E_{i,t} + \alpha_2 \Delta \ln [(1 - \widehat{v}_{i,t}) SU_{i,t}] + \alpha_3 u_{i,t-1} \\ & + \alpha_4 \Delta \ln R_{i,t-1} + \alpha_5 [\Delta \ln E_{i,t}] VR dummy_{i,t} + \varepsilon_{i,t} \end{aligned} \quad (7)$$

Figure 1 shows for each MSA when the prevailing vacancy rate was above or below the local long term average vacancy rate. Our hypothesis is that the impact of office employment changes on rents is higher when vacancy rates are low when compared to a less tense office market.

We estimate and evaluate models (6) and (7) to test the effects of including the asymmetric properties based on our panel data of fifteen MSA's over 69 quarters, resulting in a sample of 1035 observations. So far the office literature has been dominated by papers focusing on explaining the rent dynamics of one single office market. Examples are London by Wheaton, Torto and Evans (1997a), Hendershott et al. (1999), and Farrelly and Sanderson Farrelly and Sanderson (2005), Stockholm by Gunnelin and Söderberg (2003), Englund et al. (2008a, b), Sydney by Hendershott (1996), San Francisco by Rosen (1984), Hong Kong by Hui and Yu (2006), Dublin by D'Arcy et al. (1999), and Boston by McClure (1991).

Few studies exist that analyze multiple markets. D'Arcy et al. (1997) examine 22 European cities and use pooled analysis with city dummies based on size of office stock, growth of real GDP and growth in service sector employment. Giussani et al. (1992) estimate rent models for ten European cities. Different demand side variables are tested in a pooled regression and for the individual cities. They find that coefficients are comparable in sign and magnitude across cities. Hendershott et al. (2002) estimate panel data error correction models for retail and office property rents for eleven regions in the U.K. covering 29 years. They estimate separate regional models and combine regions in panels based on communality in income and price elasticities. The main finding is that, while economic divers can vary between regions, that there is no evidence of differences in the operation of the regional property markets outside London. De Wit and van Dijk (2003) test rent models for static and dynamic panels for 46 office district across Asia, Europe and the U.S. and up to 56 quarterly observations per district.

Data

The data set in this study consists of quarterly, MSA level, real estate and employment data covering the period 1990-2007. Torto Wheaton Research (TWR) is the source of our real estate data which combines an extensive geographical coverage with a broad set of relevant real estate data. For the 15 largest office markets in the U.S. we have data on office completions, net absorption of office space, the net rentable area of office space in the MSA, office market vacancy rates and the TWR office rent index.⁵ Data on office completions reflects the square

⁵ The data gathering and compilation methodology of TWR has been discussed in detail in Wheaton et al. (1997b).

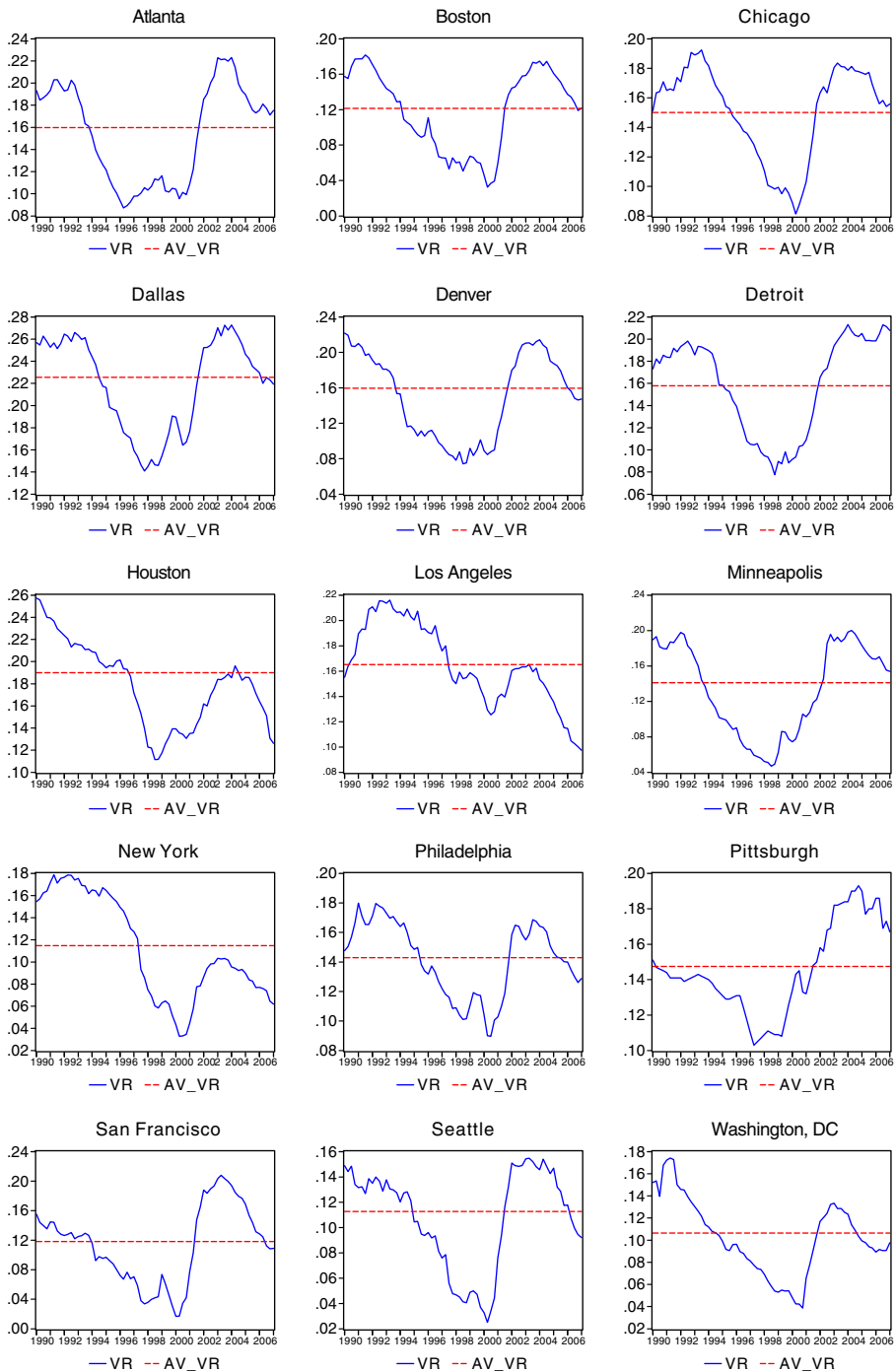


Fig. 1 Vacancy rates and MSA average vacancy rates. This figure shows the quarterly vacancy rate (VR) on a MSA level and the local average vacancy rate (AV_VR) over the study period 1990-2007

footage of office space completed each period or new space under construction due to completion in near future. The figure on net absorption reflects the net change in competitively leased space per period in square feet. The square footage is the amount of new space being brought into a market over a period of time, minus the change in vacant space over that same time period. Net rentable area data contain all office buildings whose size exceeds for most markets 20,000 or 30,000 square feet and results from information gathered by local CB Commercial offices throughout the United States. Information on office market vacancy rates is the result of an extensive survey by CB Commercial, which covers the vast majority of competitively rented buildings.

Different forms of office rent indices have been applied in extant literature. Private companies that provide the data apply different methodologies when constructing indices and face the problem of determining the true rent paid on a contract. This problem is caused by the incentive that property owners and tenants have not to disclose rent rates as this would limit future negotiation bandwidths. Furthermore, property owners offer all kinds of incentives in cash and kind to attract potential tenants. As the value of the incentives is positively related to the prevalent vacancy rate there is no fixed adjustment possible over time. McDonald (2002) discusses five different measures of rent per square foot that have been employed in empirical office market research and ranks the different rent indices in increasing accuracy as follows: [I] asking rent (gross and net), [II] face rent on new leases (gross and net), [III] consideration rent averaged over the term of the lease (rent levels are adjusted for broker commission and months of free rent but both on gross and net basis) [IV] consideration rent index (corrected for building and contract details) and [V] effective net rent that measures the net present value of cash flows over the term of the lease. The TWR office rent index that we use in our study is of type [IV] and is based on information contained in CB Commercial deals. Sivitanides (1997) and Mourouzi-Sivitanidou (2002) are examples of papers that use data by the same provider which is based on hedonic methodology as employed by Wheaton and Torto (1994) and Webb and Fisher (1996). Englund et al. (2008b) create a similar hedonic rent index for Stockholm for the period 1972-2002.

Being at the heart of the negotiations and deals provides CB Commercial with a broad set of contract and building details that subsequently enter the office rent index in the form of control variables. The basic rent specification equation is as follows:

$$\log(R) = \alpha_0 + \alpha_1 SQFT + \alpha_2 TERM + \alpha_3 HIGH + \alpha_4 NEW + \alpha_5 GROSS + \sum_{i=1979}^{1993} \beta_i D_i + 30 \sum_{j=1}^{30} \delta_j S_j, \quad (8)$$

where;

R	<i>total consideration rent per square foot per year</i>
$SQFT$	<i>square feet of lease</i>
$TERM$	<i>length of the lease in years</i>
$HIGH$	<i>dummy variable (1 for 5 + stories, 0 otherwise)</i>
NEW	<i>dummy variable (1 for new building, 0 otherwise)</i>
$GROSS$	<i>dummy variable (1 for gross rent, 0 otherwise)</i>

D_i *dummy variable for each period*
 S_j *dummy variable for up to 30 submarkets in MSA*

The TWR rent index which is used in this study exhibits the rent for a five year, 10,000 ft gross rent lease in an existing building which is located in an average area in the MSA. The rent modeling presented in this study is based on real, instead of the reported nominal, rent levels. The U.S. Bureau of Labor Statistics provides consumer price indices (CPI) on a detailed MSA level which we use to adjust the nominal rent indices. The MSA level CPI is constructed with the first quarter of 1987 as base level, therefore all reported real rent levels are in Q1 1987 dollar values.

Our model of office rent changes builds upon changes in real estate variables and an office space demand factor. In line with existing literature we measure demand for office space as the number of people employed in office occupying industries. We gather employment data from the U.S. Bureau of Labor Statistics which provides a detailed overview of MSA level employment for a broad range of industry classifications. The definition of what employment sectors constitute office demand is not uniform across studies of office market dynamics. An extensive literature study of measures of office employment shows that most studies use employment in finance, insurance and real estate (FIRE), and service industries as a proxy for office employment. This type of office employment definition is used by for example Hekman (1985), Wheaton (1987), Wheaton et al. (1997b), Sivitanides (1997), Sivitanides (1998), Shilton (1998) Hendershott et al. (1999), Mourouzi-Sivitanidou (2002)⁶, Hendershott et al. (2002), Farrelly and Sanderson (2005), and Englund et al. (2008a, b). Other studies use a narrower approximation of office employment which only includes FIRE industries (see for example Rosen (1984), Hui and Yu (2006) and Pollakowski et al. (1992). Modeling office rents for small geographic areas such as financial heart of London (a.k.a. “The City”) or the financial district of Manhattan is probably well approximated with the narrower definition of office employment. However, for broader geographic areas, such as the MSA’s we use in this study, we propose the broader measure such as employed in the majority of office rent studies. Figure 2 provides an overview of the industries that make up office employment according to the definition we use in this study.

The weight of professional and business service employment in total office employment, measured as the sum of FIRE and service sector employment, is on average 0.67 for all 15 MSA’s. The weight ranges between 0.58 for New York, a MSA with a strong financial and thus FIRE employment base, and 0.77 for Washington DC where services play a relatively large role. The service component of office employment increased for all MSA’s over the study period. The average change in FIRE employment is 21% between 1990 and 2007 (–8% in New York, up to 54% in Denver) while the average change in professional and business services is 54% (18% in Pittsburgh and 120% in Dallas). The average change across MSA’s in total office employment over our study period is 42%.

One potential problem with the office employment data is the strong seasonal component in the “administration and support and waste management and

⁶ She includes the ratio of FIRE to other office employment to take account on the idea that FIRE employment takes more square feet per employee.

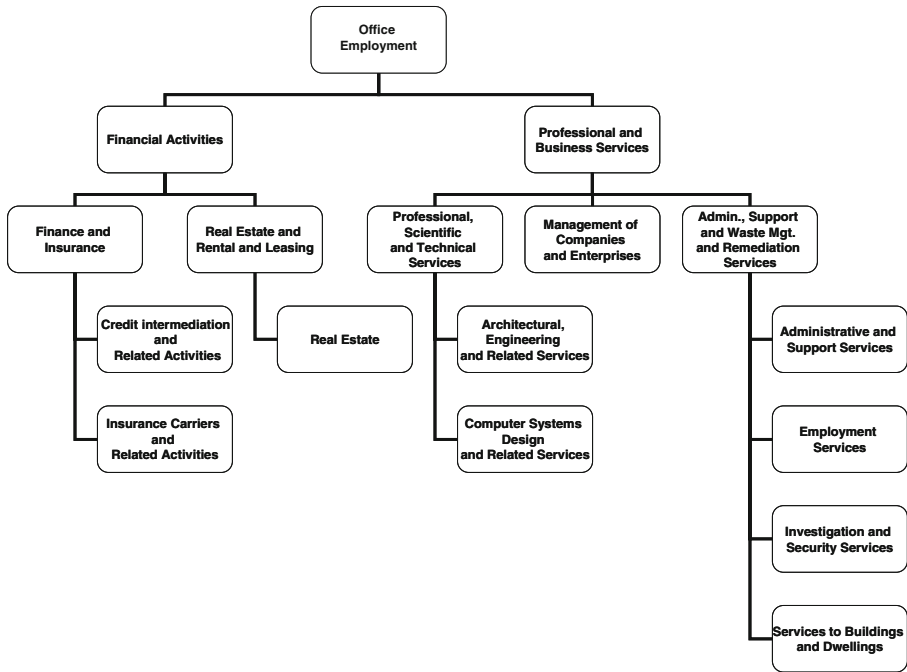


Fig. 2 Office employment make-up. This figure shows the composition of office employment. Office employment is defined as number of employees occupied in financial activities and professional and business services. Moving down through the figure each line combines the upper industry with the sub-industries it is composed of

remediation services” industry which works through to the overall office employment figure. In a perfect market companies would adjust their demand for space on a frequent basis; thereby minimizing rent costs. However, companies cannot adjust their space demand continuously due to moving costs, search time and long-term contracts. For this reason we expect companies to maximize their utility by renting floor space that lies somewhere between the maximum and minimum requirement to house all employees over contract duration. To overcome the impact of seasonality on our demand variable we use a four quarter moving average measure for the industry with high seasonal changes.⁷

Table 1 shows the correlation between changes in office employment for the whole country, the weighted average of MSA’s included in this study⁸, and the individual MSA’s. The average correlation of changes in employment across all MSA’s is 0.48; reflecting strong differences in employment growth or composition across the sample. The table shows that the Atlanta, Detroit, Houston, Los Angeles and Pittsburgh are the MSA’s with on average the lowest correlation with other markets and that these are the only MSA’s that exhibit statistically non-significant correlations.

⁷ We also tried the U.S. Statistics Bureau X12 procedure to delete the seasonality, but despite its theoretical superiority, peaks and troughs remain which does not fit demand for real estate assets.

⁸ Where weights are based on the number of people employed in office occupying industries.

Table 1 Correlation change in office employment

	Total US	15 MSAs	Atlanta	Boston	Chicago	Dallas	Denver	Detroit	Houston	Los Angeles	Minneapolis	New York	Philadelphia	Pittsburgh	San Francisco	Seattle	Washington, DC
Total US	1	.829(**)	.656(**)	.732(**)	.663(**)	.763(**)	.653(**)	.539(**)	.355(**)	.473(**)	.545(**)	.704(**)	.670(**)	.245(*)	.618(**)	.693(**)	.554(**)
15 MSAs		1	.642(**)	.896(**)	.786(**)	.831(**)	.725(**)	.552(**)	.533(**)	.640(**)	.673(**)	.910(**)	.734(**)	.446(**)	.699(**)	.781(**)	.722(**)
Atlanta			1	.569(**)	.611(**)	.568(**)	.591(**)	.592(**)	0.162	0.220	.484(**)	.481(**)	.417(**)	0.219	.439(**)	.450(**)	.339(**)
Boston				1	.710(**)	.681(**)	.674(**)	.457(**)	.460(**)	.499(**)	.664(**)	.827(**)	.620(**)	.443(**)	.617(**)	.674(**)	.645(**)
Chicago					1	.666(**)	.659(**)	.506(**)	.450(**)	.370(**)	.589(**)	.601(**)	.588(**)	.286(*)	.498(**)	.580(**)	.459(**)
Dallas						1	.672(**)	.430(**)	.605(**)	.429(**)	.504(**)	.704(**)	.612(**)	.331(**)	.676(**)	.751(**)	.490(**)
Denver							1	.468(**)	.491(**)	.273(*)	.583(**)	.571(**)	.454(**)	.276(*)	.658(**)	.682(**)	.379(**)
Detroit								1	0.112	.342(**)	.432(**)	.354(**)	.279(*)	0.088	.340(**)	.359(**)	.297(*)
Houston									1	.275(*)	.279(*)	.399(**)	.412(**)	0.199	.522(**)	.569(**)	.298(*)
Los Angeles										1	.297(*)	.563(**)	.345(**)	0.131	.311(**)	.401(**)	.449(**)
Minneapolis											1	.593(**)	.424(**)	.301(*)	.481(**)	.541(**)	.358(**)
New York												1	.701(**)	.480(**)	.551(**)	.674(**)	.706(**)
Philadelphia													1	.429(**)	.399(**)	.645(**)	.612(**)
Pittsburgh														1	.280(*)	.448(**)	.482(**)
San Francisco															1	.645(**)	.456(**)
Seattle																1	.491(**)
Washington, DC																	1

This table shows the correlation of changes in office employment between pairs of MSA's, the national change in office employment (Total U.S.) and an employment weighted average of the 15 MSA's included in the study (15 MSAs). (**) and (*) indicate significance at 0.01 and 0.05 levels respectively

Table 2 provides an overview of summary statistics of office data for the 15 MSA's covered in this study. New York is by far the largest office market at the end of 2006 with a total square footage of over 400 million; over 60% larger than the second in line, Los Angeles and more than 6.5 times the size of Minneapolis which is the smallest office market covered in this study. Average real rents in 1987 constant dollars range between \$9.7 in Houston and \$24.4 in New York. Summary statistics for the vacancy rate show that all cities, when examining the mean over the study period, report double digit vacancy rates. Vacancy rates over the study period range between 1.7%, in San Francisco near the end of the Dotcom boom, to 30.3% in Houston towards the end of the 1980's.

Figure 3 displays the time series of vacancy rates; real rent levels and the number of employees in office occupying industries over the period 1990–2007. The Figure shows that the vacancy rate for all MSA's over the study period is often a close mirror image of real rent index despite the disturbing influence of new construction and hidden vacancy rates, as discussed in Englund et al. (2008b). Vacancy rates show similar patterns across all MSA's and are characterized by high but steady levels over the years 1988–1994, which was a period characterized by a downturn in the U.S. economy partly due to the collapse of the junk bond market and a credit crunch. Over the whole, vacancy rates decreased over the period 1995–1998 preceding a period of low vacancy rates during the economic boom period 1998–2000. The latter period clearly shows the non-negativity constraint of vacancy rates as vacancies reached their local minima during the years 1998–2000, triggering new construction and the lowest space usage per employee over the study period as shown in Fig. 4.⁹

After the turn of the millennium the U.S. economy hit hard times with the crash of the Dotcom bubble and the September 11 attacks on New York and Washington DC. The combination of ongoing new supply and decreasing employment at office occupying companies in all 15 MSA's lead to a steep increase in vacancy rates over the period 2000–2003.

Real rent levels show similar patterns across MSA's over time. Rent expressed in constant 1987 dollars show large dispersion across cities. In the first quarter of 2000 real rent levels were as low as \$11.29 in Houston, which alternates with Denver for the lowest rent per square foot and as high as \$28.51 in New York, where renting office space was most expensive over the whole study period. The discrepancy between the highest and lowest rent values is fairly consistent over time. On average the highest rent is 2.64 times the lowest rent over all quarters with a range of 2.1 to 3.6 over the study period.

Empirical Results

This section presents the results for the two stage error correction model for changes in real office rents. One of the contributions of this study is the addition of a test of asymmetry in rent response to positive changes in office employment. Therefore we

⁹ We measure space usage per employee in square feet as: $(\text{net rentable area} \times (1 - \text{vacancy rate})) / \text{office employment}$.

Table 2 Descriptive statistics

MSA	Mean	Min.	Year / Quarter	Min	Max	Year / Quarter	Max
Panel A							
Atlanta	97,534	65,299	88Q1		126,691	07Q1	
Boston	134,036	110,054	88Q1		154,920	07Q1	
Chicago	193,125	160,835	88Q1		218,883	07Q1	
Dallas	119,491	107,327	88Q1		139,324	07Q1	
Denver	72,428	64,437	88Q1		85,372	07Q1	
Detroit	62,018	50,664	88Q1		70,391	07Q1	
Houston	127,040	121,447	88Q1		137,171	07Q1	
Los Angeles	159,395	129,121	88Q1		173,390	07Q1	
Minneapolis	57,723	47,998	88Q1		65,113	06Q4	
New York	418,706	397,501	88Q1		427,568	07Q1	
Philadelphia	87,196	68,891	88Q1		100,200	07Q1	
Pittsburgh	59,027	53,050	88Q1		65,274	06Q4	
San Francisco	73,119	63,071	88Q1		83,542	07Q1	
Seattle	61,192	43,793	88Q1		75,599	07Q1	
Washington, DC	211,601	159,481	88Q1		262,044	07Q1	
All	128,909	43,793			427,568		
Panel B							
Atlanta	11.6	10.0	93Q2		13.1	88Q2	
Boston	17.0	12.8	92Q4		27.0	00Q4	
Chicago	15.2	12.9	05Q3		18.3	88Q2	
Dallas	11.0	9.1	93Q4		14.6	98Q4	
Denver	9.8	8.2	91Q4		12.8	00Q2	
Detroit	11.0	9.1	07Q1		14.1	88Q4	
Houston	9.7	8.3	93Q4		11.6	00Q3	
Los Angeles	13.6	11.3	95Q1		17.0	88Q1	
Minneapolis	14.5	11.7	92Q4		18.3	88Q2	
New York	24.4	18.3	93Q4		34.6	01Q1	
Philadelphia	12.5	10.2	06Q3		16.2	89Q4	
Pittsburgh	11.7	9.6	06Q3		13.1	00Q2	
San Francisco	14.1	10.9	05Q1		23.1	00Q2	
Seattle	14.3	12.2	04Q4		18.6	98Q4	
Washington, DC	17.8	14.5	93Q2		23.5	00Q4	
All	13.9	8.2			34.6		
Panel C							
Atlanta	16.0%	8.7%	96Q2		22.3%	04Q1	
Boston	12.1%	3.3%	00Q2		18.2%	91Q3	
Chicago	15.0%	8.1%	00Q2		19.2%	93Q3	
Dallas	22.5%	14.1%	97Q4		28.3%	88Q2	
Denver	16.0%	7.4%	98Q3		27.3%	88Q1	
Detroit	15.8%	7.8%	98Q4		21.3%	04Q1	

Table 2 (continued)

MSA	Mean	Min.	Year / Quarter	Min	Max	Year / Quarter	Max
Houston	19.0%	11.2%	98Q3		30.3%	88Q1	
Los Angeles	16.5%	9.7%	07Q1		21.6%	93Q2	
Minneapolis	14.1%	4.7%	98Q3		21.9%	88Q3	
New York	11.5%	3.3%	00Q2		17.9%	91Q2	
Philadelphia	14.3%	9.0%	00Q3		18.0%	91Q1	
Pittsburgh	14.7%	10.3%	97Q2		19.3%	04Q4	
San Francisco	11.8%	1.7%	00Q1		20.8%	03Q2	
Seattle	11.3%	2.5%	00Q2		17.2%	89Q2	
Washington, DC	10.6%	3.9%	00Q4		17.4%	91Q2	
All	14.7%	1.7%			30.3%		

This table shows descriptive office market statistics for 15 U.S. MSA's over the period 1988 till the first quarter of 2007. Panel A shows descriptive statistics for net rentable area which is the sum of rentable floor space of all office buildings in the MSA. Figures are in '000s of square feet. Panel B shows summary statistics of Torto Wheaton Research real rent (in 1987.1 constant dollars) per square foot. Panel C shows summary statistics for the vacancy rate

estimate both a symmetric and an asymmetric model specification, based on Eqs. 6 and 7 respectively. Table 3 displays the results for the full panel including all 15 MSA's. The top panel displays the results for the long run model. We base this model on non-differenced data and use it to calculate the prevailing rent disequilibrium.

The long run model does not differ between the symmetric and asymmetric model as it is merely used to determine the equilibrium rent level. Our regression results show that the long run model has an adjusted R-squared of approximately 0.80 with a Durbin Watson coefficient considerably below unity. The coefficients and model fit estimates from the long run model are comparable to the findings for European office markets as reported in Hendershott et al. (2002) and Brounen and Jennen (2009), and are a direct result of the trending variables used in the long-run model.

The bottom panel in Table 3 shows the result for the differenced rent model. In the symmetric model specification we show that rents react positively to changes in office employment and lagged changes in office rents. The coefficient for the error correction term is between zero and minus one which indicates a partial adjustment towards equilibrium over one quarter periods. The magnitude of this estimate is however very small, pointing at very slow adjustment over time.¹⁰ The measure for occupied space shows an unexpected positive sign which is however only significant at the 5% level. The second short run model specification presented in Table 3 shows the result for the asymmetric model. Coefficients in the asymmetric model are similar to the results in the symmetric model in both sign and statistical significance, but with an even lower statistical significance for the occupied space variable. The

¹⁰ The error correction term is -0.008 in the symmetric model for the whole panel. This number implies that over the course of one year only 3.23% of the disequilibrium in rents is restored.

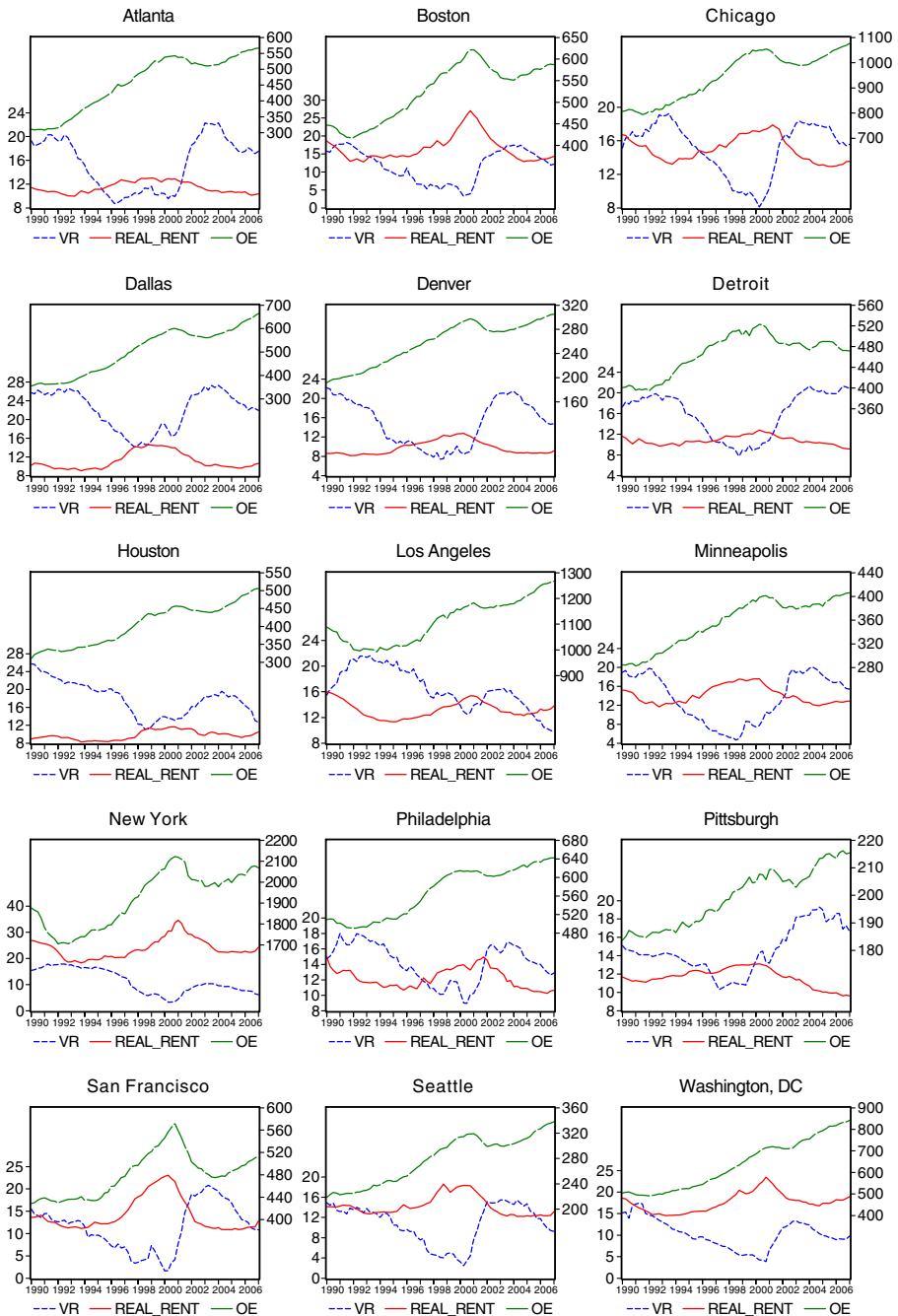


Fig. 3 Office market dynamics. This figure shows the dynamics in vacancy rate (VR, left axis in %), the Torto Wheaton Research office rent index in real terms (Real_rent, left axis in constant 1987.1 dollars) in \$ per square foot and office employment (OE, right axis in '000s employees) for all 15 MSA's covered in this study

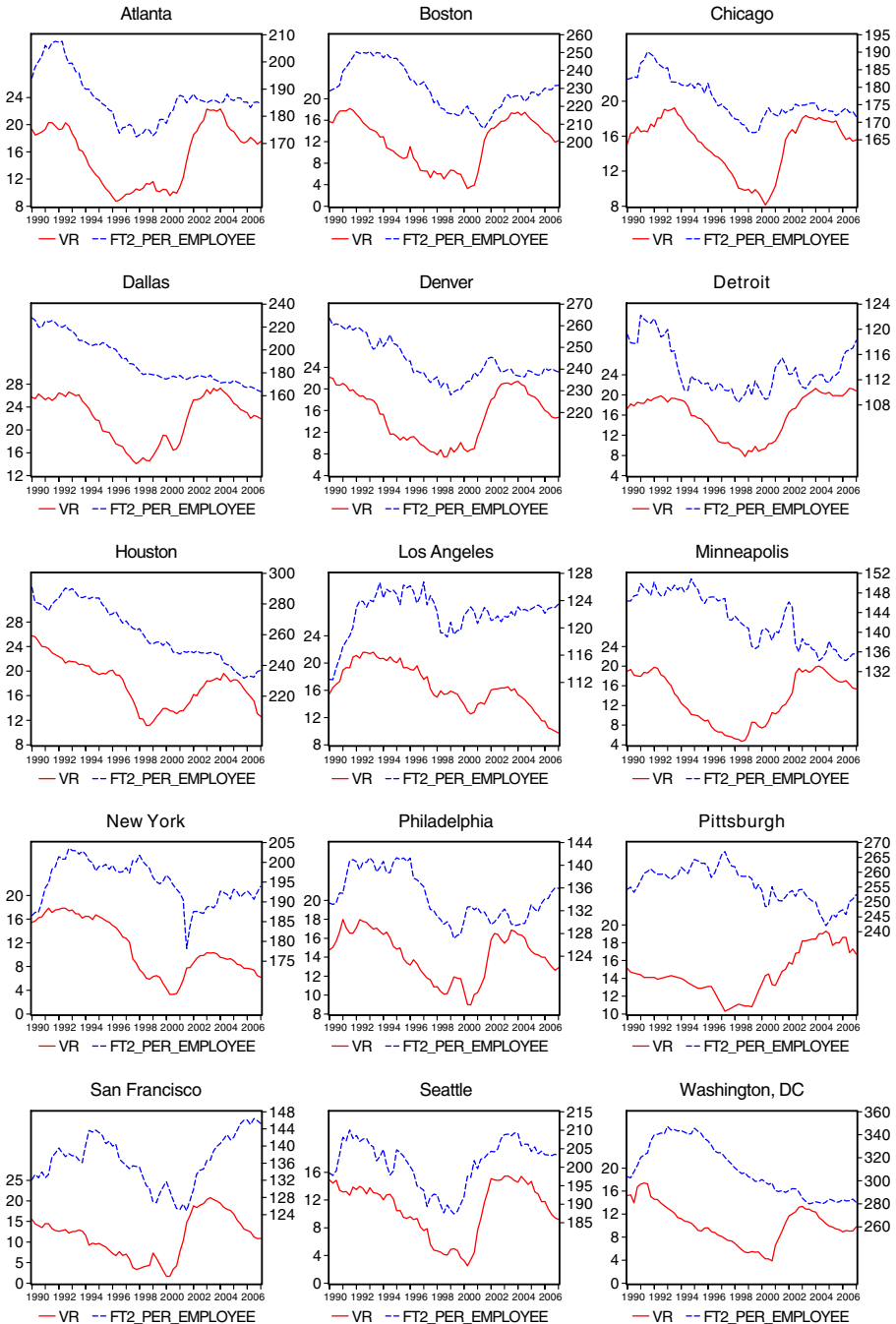


Fig. 4 Occupied office space per office employee. This figure shows vacancy rate dynamics (VR, left axis in %) and the office space usage per employee (FT2_per_employee, left axis in ft² per employee) calculated as $[(1-VR) * \text{net rentable floor space}] / \text{office employment}$

Table 3 Regression results (all cities)

	All City Panel	
	Symmetric Model	Asymmetric Model
Long-run model		
Constant	8.559 *** (0.968)	8.559 *** (0.968)
$\ln(E_t)$	1.292 *** (0.095)	1.292 *** (0.095)
$\ln[(1-\hat{v}_t)SU_t]$	-1.225 *** (0.132)	-1.225 *** (0.132)
N	990	990
R ² -adj	0.799	0.799
DW	0.060	0.060
Short-run model		
Constant	-0.002 *** (0.000)	-0.003 *** (0.000)
$\Delta \ln(E_t)$	2.499 *** (0.272)	1.503 *** (0.314)
$\Delta \ln[(1-\hat{v}_t)SU_t]$	0.584 ** (0.279)	0.156 * (0.275)
u_{t-1}	-0.008 *** (0.002)	-0.015 *** (0.002)
$\Delta \ln R_{t-1}$	-0.419 *** (0.030)	0.399 *** (0.029)
$[\Delta \ln E +_t] * VR_DUMMY_t$	—	2.406 *** (0.401)
N	975	975
R ² -adj	0.399	0.421
DW	1.913	1.918

This table reports the error correction model of office rents for a panel of 15 MSA's included in the study based on quarterly observations over the period 1990–2007. The long-run model $\ln R_t = \alpha_0 + \alpha_1 \ln E_t + \alpha_2 \ln[(1-\hat{v}_t)SU_t]$ is estimated as a cross sectional fixed effect model. The dependent variable is real office rent in 1987.1 constant U.S. dollars. We estimate office employment (E_t) as the sum of employment in finance, insurance, real estate, professional- and business services. $[(1-\hat{v}_t)SU_t]$ is an estimate for occupied space, where \hat{v} is the fitted vacancy rate based on an AR(4) model and SU is the supply of office space in square feet. The results include the symmetric and asymmetric models which differ in the short-run model only. The symmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln[(1-\hat{v}_t)SU_t] + \alpha_3 u_{t-1} + \alpha_4 \Delta \ln R_{t-1}$ is estimated as a cross sectional fixed effect model. Δ measures the one period change in variables. u_{t-1} is the one period lagged residual of the long-run model. $\Delta \ln R_{t-1}$ is the one period lagged change in real prime rents. The asymmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln[(1-\hat{v}_t)SU_t] + \alpha_3 u_{t-1} + \alpha_4 \Delta \ln R_{t-1} + \alpha_5 [\Delta \ln E +_t] VR_DUMMY_t$ is estimated as a cross sectional fixed effect model. $[\Delta \ln E +_t]$ reflects positive one period changes in office employment and takes value zero if the change in employment is negative. VR_DUMMY_t is a dummy variable that takes value 1 if the vacancy rate in time t is below the MSA average vacancy rate, and 0 otherwise. DW is the Durbin-Watson statistic. Standard error statistics appear in parentheses. ***, **, * indicate significance at the 1%, 5% and 10% level respectively.

positive and significant coefficient for the asymmetry variable shows that rents react significantly stronger to positive changes in office employment when vacancy rates are below the long term average, when compared to times of abundant vacant space. This finding is in line with expectations. If vacancy rates are high, new demand for space will first alleviate the owners of non-income producing vacant space before a clear effect on office rents is visible. When vacancy rates are low the effect of additional demand for office space as a result of an increase in office employment is more directly related to office rents. However, including this asymmetric element in the model enhances the fit of the model only marginally.

Cluster Analysis

The panel results presented in Table 3 assume that the coefficients for the independent variables are equal across all MSA's. In order to relax this assumption we create panels based on similarity in the pattern of rent and office employment changes over the sample period. In this way we are able to maintain the benefit of large sample sizes, examine clusters with maximum between cluster heterogeneity, while keeping the within sample homogeneity as large as possible. Hendershott et al. (2002) is the only other known study that groups regions based on some similarity. Their paper studies rent changes for a range of regions and estimates separate models for "London" and "Other" regions in the UK for 11 regions and 29 years. Clusters in the Hendershott et al. (2002) paper are based on similarities of the income and price elasticities in the long run models. In this study we use an alternative methodology in which we use multi dimensional scaling (MDS) and subsequent hierarchical clustering analysis to group MSA in two clusters based on similarities in changes in rent and office employment over time. MDS is a powerful tool for visualizing correlations between pairs of cities or other instances (see for example Groenen and Franses (2000) for an application in stock market correlation analysis). MDS creates points in a low dimensional space where each dot reflects for example a city. Clusters of cities appear if dots in the low dimensional space appear close to each other in the output. The benefit over more traditional correlation analysis is the way MDS shows not only the similarity between individual pairs of instances but also the way in which all other observations are related. Besides the visual application, MDS output also includes common space coordinates which forms the input for the geographic representation of similarities. The common space coordinates form the input for hierarchical clustering analysis; the foundation for the actual cluster formation. We test different dimensional settings for the MDS and found, according to the guidelines by Kruskal (1964), that the use of three dimensions is optimal in our study. Our clusters based on communalities in rent and office employment changes over the study period are shown in Fig. 4. Panels A and B show the clusters based on rent and employment changes, respectively. Based on real rent changes we form two clusters. One cluster consists of Boston, New York and San Francisco (further indicated as cluster A2) and the other cluster encompasses all other MSA's (cluster A1).

If we base the clusters on office employment changes, Fig. 5 shows that three main clusters arise. One cluster consists of Atlanta and Detroit (cluster B3), a second

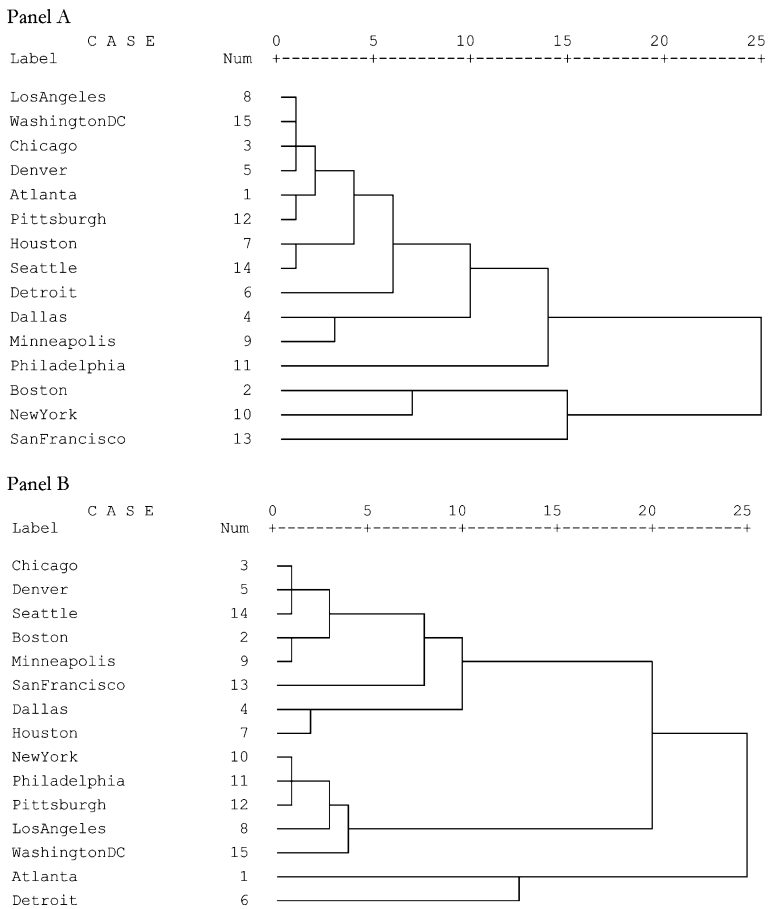


Fig. 5 Hierarchical clusters. This figure shows the dendrogram which results after a hierarchical clustering analysis based on three dimensional common space coordinates. Common space coordinates are constructed with multi dimensional scaling. Panel A shows clusters based on changes in office rents and Panel B shows clusters based on changes in office employment

cluster includes New York, Philadelphia, Pittsburg, Los Angeles and Washington DC (cluster B2) and the third cluster consists of the remaining MSA's (cluster B1).¹¹

Panel A1 in Table 4 shows the results for cluster A1. Coefficients and signs are comparable to the findings presented in Table 3 with a model fit that is slightly lower than the result for a panel including all MSA's. The error correction term shows that rent very slowly adjust towards equilibrium over the term of one quarter; a finding shared with all other model specifications presented in this study. Results of the short run model show that the impact of changes in our estimate of occupied space is not statistically different from zero. Again, we show that the rent adjustment as a result

¹¹ One interesting finding from this clustering methodology based on similarities in office rent or employment changes is that clusters are not in line with geographic locations of the MSA's. Further analysis could provide more insight into the driving forces behind the correlations; possible causes are similarities in local GDP drivers or employment composition.

Table 4 Regression results for clusters based on communality in office rent changes

	Panel A1		Panel A2	
	Symmetric Model	Asymmetric Model	Symmetric Model	Asymmetric Model
Long-run model				
Constant	6.238 *** (0.915)	6.238 *** (0.915)	13.566 *** (2.725)	13.566 *** (2.725)
$\ln(E_t)$	0.896 *** (0.091)	0.896 *** (0.091)	3.071 *** (0.255)	3.071 *** (0.255)
$\ln[(1-\hat{v}_t)SU_t]$	-0.812 *** (0.126)	-0.812 *** (0.126)	-2.625 *** (0.352)	-2.625 *** (0.352)
N	792	792	198	198
R ² -adj	0.752	0.752	0.784	0.784
DW	0.055	0.055	0.119	0.119
Short-run model				
Constant	-0.002 *** (0.000)	-0.003 *** (0.000)	-0.002 *** (0.001)	-0.003 *** (0.001)
$\Delta \ln(E_t)$	2.121 *** (0.293)	0.774 ** (0.345)	3.897 *** (0.678)	3.139 *** (0.771)
$\Delta \ln[(1-\hat{v}_t)SU_t]$	0.456 (0.307)	0.413 (0.298)	0.901 (0.651)	0.886 (0.645)
u_{t-1}	-0.009 *** (0.003)	-0.021 *** (0.003)	-0.012 ** (0.005)	-0.015 *** (0.005)
$\Delta \ln R_{t-1}$	-0.400 *** (0.034)	0.362 *** (0.033)	0.415 *** (0.068)	0.411 *** (0.067)
$[\Delta \ln E + \hat{v}] \cdot VR_DUMMY_t$	—	2.962 *** (0.429)	—	2.314 ** (1.153)
N	780	780	195	195
R ² -adj	0.333	0.372	0.543	0.550
DW	1.897	1.907	1.936	1.944

This table reports the error correction model of office rents for a panel of 15 MSA's included in the study based on quarterly observations over the period 1990–2007. The sample is split in two Panels based on communality in office rent changes. The long-run model $\ln R_t = \alpha_0 + \alpha_1 \ln E_t + \alpha_2 \ln[(1-\hat{v}_t)SU_t]$ is estimated as a cross sectional fixed effect model. The dependent variable is real office rent in 1987.1 constant U.S. dollars. We estimate office employment (E_t) as the sum of employment in finance, insurance, real estate, professional- and business services. $[(1-\hat{v}_t)SU_t]$ is an estimate for occupied space, where \hat{v}_t is the fitted vacancy rate based on an AR(4) model and SU_t is the supply of office space in square feet. The results include the symmetric and asymmetric models which differ in the short-run model only. The symmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln[(1-\hat{v}_t)SU_t] + \alpha_3 u_{t-1} + \alpha_4 \Delta \ln R_{t-1}$ is estimated as a cross sectional fixed effect model. Δ measures the one period change in variables. u_{t-1} is the one period lagged residual of the long-run model. $\Delta \ln R_{t-1}$ is the one period lagged change in real prime rents. The asymmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln[(1-\hat{v}_t)SU_t] + \alpha_3 u_{t-1} + \alpha_4 \Delta \ln R_{t-1} + \alpha_5 [\Delta \ln E + \hat{v}] VR_DUMMY_t$ is estimated as a cross sectional fixed effect model. $[\Delta \ln E + \hat{v}]$ reflects positive one period changes in office employment and takes value zero is the change in employment is negative. VR_DUMMY_t is a dummy variable that takes value 1 if the vacancy rate in time t is below the MSA average vacancy rate, and 0 otherwise. DW is the Durbin-Watson statistic. Standard error statistics appear in parentheses. ***, **, * indicate significance at the 1%, 5% and 10% level respectively

Table 5 Regression results for clusters based on communality in office employment changes

	Panel B1		Panel B2		Panel B3	
	Symmetric Model	Asymmetric Model	Symmetric Model	Asymmetric Model	Symmetric Model	Asymmetric Model
Long-run model						
Constant	8.845 ***	8.845 ***	8.984 ***	8.984 ***	7.552 ***	7.552 ***
	1.337	1.733	1.733	1.190	1.190	
ln (E_t)	1.291 ***	1.291 ***	1.251 ***	1.251 ***	1.025 ***	1.025 ***
	0.126	0.126	0.169	0.169	0.157	0.157
ln [(1- α)SU] _t	-1.247 ***	-1.247 ***	-1.226 ***	-1.226 ***	-1.029 ***	-1.029 ***
	0.179	0.179	0.233	0.233	0.189	0.189
N	552	552	345	345	138	138
R ² -adj	0.684	0.684	0.872	0.872	0.366	0.366
DW	0.058	0.058	0.075	0.075	0.146	0.146
Short-run model						
Constant	-0.003 ***	-0.003 ***	-0.002 ***	-0.003 ***	-0.002 **	-0.002 **
	0.000	0.000	0.001	0.001	0.001	0.001
Δ ln (E_t)	2.549 ***	1.707 ***	3.225 ***	1.703 **	1.299 ***	0.969
	0.382	0.482	0.579	0.829	0.601	0.748

$\Delta \ln [(1-v^*)SU_t]$	0.663 *	0.591	0.979 *	0.826	0.577	0.579
u_{t-1}	0.382	0.379	0.553	0.552	0.772	0.773
	-0.013 ***	-0.016 ***	-0.004	-0.008 *	-0.018 *	-0.020 *
$\Delta \ln R_{t-1}$	0.003	0.003	0.004	0.005	0.011	0.011
	-0.464 ***	0.456 ***	0.325 ***	0.306 ***	0.259 ***	0.254 ***
$[\Delta \ln E +] * VR_DUMMY_t$	0.042	0.041	0.055	0.055	0.087	0.087
	—	1.586 ***	—	2.481 **	—	0.593
N	520	520	325	325	130	130
R ² -adj	0.463	0.469	0.307	0.318	0.189	0.187
DW	1.795	1.809	1.981	1.969	1.572	1.581

This table reports the error correction model of office rents for a panel of 15 MSA's included in the study based on quarterly observations over the period 1990–2007. The sample is split in two Panels based on communality in office employment changes. The long-run model $\ln R_t = \alpha_0 + \alpha_1 \ln E_t + \alpha_2 \ln [1 - v^*] SU_t$ is estimated as a cross sectional fixed effect model. The dependent variable is real office rent in 1987.1 constant U.S. dollars. We estimate office employment (E_t) as the sum of employment in finance, insurance, real estate, professional- and business services. $[1 - v^*] SU_t$ is an estimate for occupied space, where v^* is the fitted vacancy rate based on an AR(4) model and SU_t is the supply of office space in square feet. The results include the symmetric and asymmetric models which differ in the short-run model only. The symmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln [1 - v^*] SU_t + \alpha_3 u_{t-1}$ is estimated as a cross sectional fixed effect model. Δ measures the one period change in variables. u_{t-1} is the one period lagged residual of the long-run model. $\Delta \ln R_{t-1}$ is the one period lagged change in real prime rents. The asymmetric short-run model $\Delta \ln R_t = \alpha_0 + \alpha_1 \Delta \ln E_t + \alpha_2 \Delta \ln [1 - v^*] SU_t + \alpha_3 u_{t-1} + \alpha_4 \Delta \ln R_{t-1} + \alpha_5 [\Delta \ln E +] VR_DUMMY_t$ is estimated as a cross sectional fixed effect model. $[\Delta \ln E +]$ reflects positive one period changes in office employment and takes value zero is the change in employment is negative. VR_DUMMY_t is a dummy variable that takes value 1 if the vacancy rate in time t is below the MSA average vacancy rate, and 0 otherwise. DW is the Durbin-Watson statistic. Standard error statistics appear in parentheses. ***, **, * indicate significance at the 1%, 5% and 10% level respectively

of an increase in office employment, the asymmetric model specification, is stronger when vacancy rates are below their long term averages. The results for the remaining MSA's, as presented under Panel A2 in Table 4, are largely comparable in sign and magnitude with a strong increase in model fit when compared to the panel of all MSA and panel A1.

Table 5 shows the results for the clusters based on communalities in changes in office employment across MSA's. Panels B1 and B2 are comparable to the results presented in Tables 3 and 4. Overall we find that all included variables are statistically significant with expected signs but also show that the variable that measures occupied space is hardly or not significant. Panel B3 stands out with model fit considerably below the other model specifications in both the long-run and the short-run model. Changes in office employment, office demand and the asymmetry measure are not significant for asymmetric model specification presented for cluster B3 while they are for most other specifications.

Conclusion

In this paper we use an error correction model for understanding the changes in real office rents for a panel of 15 U.S. MSA's over the period 1990–2007. We find that office rents react positively to a rise in office employment, lagged changes in office rents and that there is only very slow error correction towards estimated equilibrium rents. Given the non-negativity constraint of vacancy rates we extend the model by examining whether rents react to changes in employment conditional on the vacancy rate. Our results show that office rents react significantly stronger to increases in employment when vacancy rates are below the long-term average. We relax the assumption that all MSA's exhibit the same reaction to changes in independent variables by introducing results based on clustering. We base clusters on similarities in changes in rent and office employment with multi dimensional scaling. Generally we find that there are large differences in model fit across the clusters we examined but that there are only small and insignificant differences in coefficients across clusters. We thus conclude that the cluster results confirm the results found for the panel that includes all MSA's.

Acknowledgements The authors would like to thank Peter Englund and other participants in the Cambridge-UNC Charlotte-Amsterdam Symposium 2008 in Amsterdam, for their helpful feedback. Furthermore we would like to thank the editors of the JREFE Special Issue, Richard Buttner, Erasmo Giambona and Kanak Patel for their comments. We are grateful to Torto Wheaton Research for sharing their valuable data with us.

Open Access This article is distributed under the terms of the Creative Commons Attribution Noncommercial License which permits any noncommercial use, distribution, and reproduction in any medium, provided the original author(s) and source are credited.

References

- Brounen, D., & Jennen M. (2009), Office rent determinants: a tale of ten cities, *Journal of Real Estate Finance and Economics*, forthcoming.
- D'Arcy, E., McGough, T., & Tsolacos, S. (1997). National economic trends, market size and city growth effects on European office rents. *Journal of Property Research*, 14(4), 297–308.

- D'Arcy, E., McGough, T., & Tsolacos, S. (1999). An econometric analysis and forecasts of the office rental cycle in the Dublin area. *Journal of Property Research*, 16(4), 309–321.
- De Wit, I., & van Dijk, R. (2003). The global determinants of direct office real estate returns. *Journal of Real Estate Finance and Economics*, 26(1), 27–45.
- Englund P., Gunnelin Å., Hendershott P. H., & Söderberg B. (2008a). Asymmetries in property space market adjustment, *Paper presented at the Rotterdam School of Management real estate symposium*.
- Englund, P., Gunnelin, Å., Hendershott, P. H., & Söderberg, B. (2008b). Adjustment in property space markets: taking long-term leases and transaction costs seriously. *Real Estate Economics*, 36(1), 81–109.
- Farrelly, K., & Sanderson, B. (2005). Modeling regime shifts in the city of London office rental cycle. *Journal of Property Research*, 22(4), 325–344.
- Giussani, B., Hsia, M., & Tsolacos, S. (1992). A comparative analysis of the major determinants of office rental values in Europe. *Journal of Property Valuation and Investment*, 11, 157–173.
- Groenen, P. J. F., & Franses, P. H. (2000). Visualizing time-varying correlations across stock markets. *Journal of Empirical Finance*, 7, 155–172.
- Gunnelin, Å., & Söderberg, B. (2003). Term structures in the office rental market in Stockholm. *Journal of Real Estate Finance and Economics*, 26(2/3), 241–265.
- Hekman, J. S. (1985). Rental price adjustments and investment in the office market. *AREUEA Journal*, 13 (1), 32–47.
- Hendershott, P. H. (1996). Rental adjustment and valuation in overbuilt markets: Evidence from the Sydney office market. *Journal of Urban Economics*, 39, 51–67.
- Hendershott, P. H., Lizieri, C. M., & Matysiak, G. A. (1999). The Workings of the London office market. *Real Estate Economics*, 27(2), 365–387.
- Hendershott, P. H., MacGregor, B., & White, M. (2002). Explaining real commercial rents using an error correction model with panel data. *Journal of Real Estate Finance and Economics*, 24(1/2), 59–87.
- Hui, E. C. M., & Yu, K. H. (2006). The dynamics of Hong Kong's office rental market. *International Journal of Strategic Property Management*, 10, 145–168.
- Kruskal, J. B. (1964). Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis. *Psychometrika*, 29(1), 1–27.
- Levin, A., Lin, C. F., & Chu, S. S. (2002). Unit root tests in panel data: Asymptotic and finite sample properties. *Journal of Econometrics*, 108, 1–24.
- McClure, K. (1991). Estimating occupied office space: comparing alternative forecast methodologies. *The Journal of Real Estate Research*, 6(3), 305–314.
- McDonald, J. F. (2002). A survey of econometric models of office markets. *Journal of Real Estate Literature*, 10(2), 223–242.
- Mourouzi-Sivitanidou, R. (2002). Office rent processes: The case of U.S. metropolitan markets. *Real Estate Economics*, 30(2), 317–344.
- Pollakowski, H. O., Wachter, S. M., & Lynford, L. (1992). Did office market size matter in the 1980s? A time-series cross sectional analysis of metropolitan area office markets. *AREUEA Journal*, 20(1), 303–324.
- Rosen, K. T. (1984). Toward a model of the office building sector. *AREUEA Journal*, 12(3), 261–269.
- Shilton, L. (1998). Patterns of office employment cycles. *Journal of Real Estate Research*, 15(3), 339–354.
- Sivitanides, P. S. (1997). The rent adjustment process and the structural vacancy rate in the commercial real estate market. *Journal of Real Estate Research*, 13(2), 195–209.
- Sivitanides, P. S. (1998). Predicting office returns: 1997–2001. *Real Estate Finance*, 15(1), 33–42.
- Webb, R. B., & Fisher, J. D. (1996). Development of an effective rent (lease) index for the Chicago CBD. *Journal of Urban Economics*, 39(1), 1–19.
- Wheaton, W. C. (1987). The cyclic behavior of the national office market. *AREUEA Journal*, 15(4), 281–299.
- Wheaton, W. C., & Torto, R. G. (1988). Vacancy rates and the future of office rents. *Journal of the American Real Estate and Urban Economics Association*, 16(4), 430–436.
- Wheaton, W. C., & Torto, R. G. (1994). Office rent indices and their behavior over time. *Journal of Urban Economics*, 35(2), 121–139.
- Wheaton, W. C., Torto, R. G., & Evans, P. (1997a). The cyclic behavior of the Greater London office market. *Journal of Real Estate Finance and Economics*, 15(1), 77–92.
- Wheaton, W. C., Torto, R. G., & Southard, J. A. (1997b). The CB Commercial/Torto Wheaton Database. *Journal of Real Estate Literature*, 5, 59–66.